

# 2020 Semester Two (November-December 2020) Examination Period

## Faculty of Information Technology

EXAM CODES: FIT1008-FIT2085  
TITLE OF PAPER: Intro to comp science  
EXAM DURATION: 3 hours 10 mins

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## Instructions

## Marks

There are 100 marks in this exam. The exam is worth 60% of the unit mark.

## MIPS code:

- All translations from Python to MIPS must be faithful.
- Only the instructions in the MIPS reference sheet (in appendix) are allowed.
- The conventions given in the MIPS reference sheet must be followed.

## Python code:

- Unless otherwise specified, do not write type hinting, documentation, assertions or exceptions.
- Write comments if necessary for understanding the code.

## Complexity:

- By default, "runtime complexity" refers to worst-case runtime complexity, which we ask you to express using the  $O()$  notation.

# Instructions

## Information

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- By default, "runtime complexity" refers to worst-case runtime complexity, which we ask you to express using the  $O()$  notation.

# Implementations of the Set ADT

## Information

We consider the Set ADT studied in the workshop:

```
1 class Set(ABC, Generic[T]):
2     """ Abstract class for a generic Set. """
3
4     def __init__(self) -> None:
5         """ Initialization. """
6         self.clear()
7
8     @abstractmethod
9     def __len__(self) -> int:
10        """ Returns the number of elements in the set. """
11        pass
12
13    @abstractmethod
14    def is_empty(self) -> bool:
15        """ True if the set is empty. """
16        pass
17
18    @abstractmethod
19    def clear(self) -> None:
20        """ Makes the set empty. """
21        pass
22
23    @abstractmethod
24    def __contains__(self, item: T) -> bool:
25        """ True if the set contains the item. """
26        pass
27
28    @abstractmethod
29    def add(self, item: T) -> None:
30        """ Adds an element to the set. Note that an element
31        already
32        present in the set should not be added.
33        """
34        pass
35
36    @abstractmethod
37    def remove(self, item: T) -> None:
38        """ Removes an element from the set. An exception should be
39        raised if the element to remove is not present in the set.
40        """
41        pass
```

We are interested in two different implementations of this ADT and their complexities.

## Question 1

Suppose that we use an implementation of the Set ADT based on a linked list (which is not ordered). Give the runtime complexities of each of the class methods of Set for this implementation. No explanation, no marks.

6

Marks

## Question 2

Suppose that we use an implementation of the Set ADT based on an **ordered** array, which means that the internal array is kept ordered at all times:

6

Marks

```
1 class ASet(Set[T]):
2     """Implementation of the set ADT using an ordered array.
3
4     Attributes:
5         size (int): number of elements in the set
6         array (ArrayR[T]): array storing the elements of the set
7
8     ArrayR cannot create empty arrays. So default capacity value 1
9     is used to avoid this.
10    """
11
12    def __init__(self, capacity: int = 1) -> None:
13        """ Initialization. """
14        Set.__init__(self)
15        self.array = ArrayR(max(1, capacity))
```

Give the runtime complexities of each of the class methods of Set for this implementation. No explanation, no marks.

# Hash Tables

## Question 3

Consider a hash table of size `tablesize=11`, with the hash function:

$$\text{hash}(\text{key}) = \text{key} \% \text{tablesize}$$

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Marks

Starting from an empty hash table, the keys 11, 9, 7, 63, 13, 40, 33, 5, 39, 50 are inserted in the table in that order. Using Linear Probing as the method of collision resolution, and the hash function shown above, write the content of the hash table as a list. Separate the keys using commas and denote an empty slot using quotation marks (""), for instance [ x, "", y, ... ]. You must also explain each insertion step by step. **No explanation, no marks.**

## Sorting

### Question 4

Describe Selection Sort in a few sentences. How can we make Selection Sort stable? Give a precise description. How does this affect the worst-case runtime complexity? Give a proof. **No proof, no marks.**

6  
Marks

### Question 5

Describe Quicksort in a few sentences. What is the best and worst case runtime complexity of Quicksort? Give a proof of both of these. **No proof, no marks.**

6  
Marks

# Heaps

## Question 6

What are the advantages and disadvantages, if any, of an implementation of a heap that uses an array, rather than a binary tree made of linked nodes?

4

Marks

## Question 7

Consider the partial implementation of a max heap, as seen in the lessons:

6

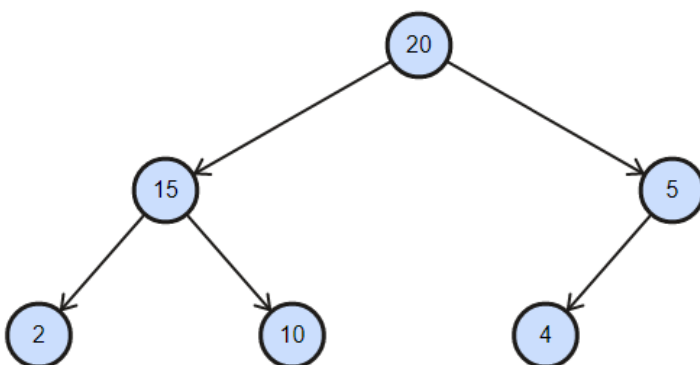
Marks

```
1 from typing import Generic
2 from referential_array import ArrayR, T
3
4 class Heap(Generic[T]):
5     MIN_CAPACITY = 1
6
7     def __init__(self, max_size: int) -> None:
8         self.length = 0
9         self.the_array = ArrayR(max(self.MIN_CAPACITY, max_size) +
10 1)
11
12     def __len__(self) -> int:
13         return self.length
```

Write a recursive method called `postorder_list()` inside the `Heap` class above that returns a list of the content of the heap binary tree in postorder traversal. Recall that in a postorder traversal of a binary tree,

- First, the left subtree is traversed recursively in postorder
- Second, the right subtree is traversed recursively in postorder
- Third, the current node is processed (in our case, this simply means that the value at the node is printed).

For example, it will return `[2, 10, 15, 4, 5, 20]` for the following `Heap` instance:





# Iterators

## Question 8

Write an iterator to generate the Fibonacci sequence. Recall that the Fibonacci sequence is 1,1,2,3,5,8,13,21, ...

Use the template:

8  
Marks

```
1 class FibIterator:
2     def __init__(self) -> None:
3
4     def __iter__(self) ->
5     FibIterator:
6
7     def __next__(self) -> T:
```

## Scoping

### Question 9

In this question you are tasked to determine what is printed by a code. Each `print` instruction prints a Python variable that refers to a function. For example, the code

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Marks

```
1 class Mystery:
2     def f(self):
3         print(f)
4
5 f = Mystery()
6 f.f()
```

prints 1 Python object, which is the function defined at line 2 (remember that in Python, functions are objects!). For the code below, write which functions (referring to them by the line at which they are defined) are printed, in the correct order. Justify each answer. No justification, no mark.

```
1 class Mystery:
2     def f(self):
3         def g():
4             print(f)
5         def h():
6             def f():
7                 print(f)
8             f()
9         g()
10        h()
11
12 f = Mystery()
13 f.f()
```

# Stack ADT and sorting

## Question 10

The problem consists in sorting a stack with the help of an auxiliary stack, and no other container. Recall that the ADT of a Stack is:

8

Marks

```
1 class StackADT(ABC, Generic[T]):
2     def __init__(self) -> None:
3         self.length = 0
4
5     @abstractmethod
6     def push(self, item: T) -> None:
7         """ Pushes an element to the top of the stack."""
8         pass
9
10    @abstractmethod
11    def pop(self) -> T:
12        """ Pops an element from the top of the stack."""
13        pass
14
15    @abstractmethod
16    def peek(self) -> T:
17        """ Pops the element at the top of the stack."""
18        pass
19
20    def __len__(self) -> int:
21        """ Returns the number of elements in the stack."""
22        return self.length
23
24    def is_empty(self) -> bool:
25        """ True if the stack is empty. """
26        return len(self) == 0
27
28    @abstractmethod
29    def is_full(self) -> bool:
30        """ True if the stack is full and no element can be pushed. """
31        pass
32
33    def clear(self):
34        """ Clears all elements from the stack. """
35        self.length = 0
```

Given one input stack and one temporary stack, write a Python program that sorts the input stack, using the temporary stack (no other containers) and without calling Python's sorting methods in any way. Comment your code. For reference, there is a solution that has fewer than 12 lines (excluding comments).

# The Bisection Algorithm

## Information

We now attempt to answer a few questions related to the bisection method for finding the square root of a number  $x$ , which we denote  $x^{1/2}$ . We provide the description of the recursive version of this algorithm here.

The input of this algorithm is:

- $x$ , a real number  $\geq 0$  that we must find the root of.
- $l$ , a lower bound on  $x^{1/2}$ , i.e.  $l \leq x^{1/2}$ . Also  $l \geq 0$ .
- $u$ , an upper bound on  $x^{1/2}$ , i.e.  $x^{1/2} \leq u$ . Also  $l \leq u$ .
- $e$ , a numerical tolerance, i.e. the output  $y$  of the algorithm should satisfy  $|y - x^{1/2}| \leq e$ .

The bisection algorithm relies on the assumption that the root that we are looking for,  $x^{1/2}$ , is in the interval  $[l, u]$  at the start of the algorithm. It recursively divides the interval by 2, and selects the half in which  $x^{1/2}$  is located by adjusting the values of  $l$  and  $u$ , until the interval is small enough to satisfy  $|u - l| \leq e$ , at which point  $u$  can be output with the guarantee that  $|u - x| \leq e$ .

A Python implementation of the bisection algorithm that uses recursion to compute  $x^{1/2}$  is:

```
1 def bisection_rec(x, l, u, e):
2     # base case
3     if u - l <= e:
4         return u
5
6     # compute the middle point of the interval [l,u]
7     m = (u+l)/2
8     # compute its square
9     s = m*m
10
11    # check how to divide the interval
12    if s >= x:
13        u = m
14    else:
15        l = m
16
17    # recurse
18    return bisection_rec(x, l, u, e)
```

Make sure that you understand this algorithm as it will be used in a few questions. The questions are independent of each other and can be attempted in any order.

Examples of calls and returned values are given below:

`bisection_rec(2, 0, 2, 0.0001)` -> 1.41424560546875

`bisection_rec(2, 0, 2, 0.1)` -> 1.4375

`bisection_rec(4.0, 0, 4.0, 0.0001)` -> 2.0

## Question 11

The Python code we have provided does not have type hinting, documentation or assertions (in this question we ignore exceptions). We provide the original code again for convenience:

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Marks

```
1 def bisection_rec(x, l, u, e):
2     # base case
3     if u - l <= e:
4         return u
5
6     # compute the middle point of the interval [l,u]
7     m = (u+l)/2
8     # compute its square
9     s = m*m
10
11    # check how to divide the interval
12    if s >= x:
13        u = m
14    else:
15        l = m
16
17    # recurse
18    return bisection_rec(x, l, u, e)
```

Based on the description of the algorithm and the code itself, add **type hinting**, **documentation** (description, pre- and post-conditions) and **assertions** to match. Do not add exceptions, but for the purpose of this question add assertions where you may normally add an exception.

## Question 12

Extend the function we have provided to handle an extra argument  $n$  and to compute and return the  $n^{\text{th}}$  root of  $x$  (rather than the square root). We provide the original code again for convenience:

3

Marks

```
1 def bisection_rec(x, l, u, e):
2     # base case
3     if u - l <= e:
4         return u
5
6     # compute the middle point of the interval [l,u]
7     m = (u+l)/2
8     # compute its square
9     s = m*m
10
11    # check how to divide the interval
12    if s >= x:
13        u = m
14    else:
15        l = m
16
17    # recurse
18    return bisection_rec(x, l, u, e)
```

### Question 13

In this question we want to determine the runtime complexity of the bisection algorithm. We provide the original code again for convenience:

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Marks

```
1 def bisection_rec(x, l, u, e):
2     # base case
3     if u - l <= e:
4         return u
5
6     # compute the middle point of the interval [l,u]
7     m = (u+l)/2
8     # compute its square
9     s = m*m
10
11    # check how to divide the interval
12    if s >= x:
13        u = m
14    else:
15        l = m
16
17    # recurse
18    return bisection_rec(x, l, u, e)
```

We denote  $L = (u - l)$  the length of the search interval and  $N = L/e$  the number of intervals corresponding to the base case.

Express the worst-case runtime complexity of this algorithm as a function of  $N$ . Justify your answer.

### Question 14

In this question we ask that you write the iterative version of the recursive bisection. We provide the original code again for convenience:

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Marks

```
1 def bisection_rec(x, l, u, e):
2     # base case
3     if u - l <= e:
4         return u
5
6     # compute the middle point of the interval [l,u]
7     m = (u+l)/2
8     # compute its square
9     s = m*m
10
11    # check how to divide the interval
12    if s >= x:
13        u = m
14    else:
15        l = m
16
17    # recurse
18    return bisection_rec(x, l, u, e)
```

Give a direct translation using the template provided.

## Question 15

Faithfully translate into MIPS the (modified) bisection function. Do not translate the body of the original function. Only translate the code below:

16  
Marks

```
1 def bisection_rec(x, l, u, e):  
2     #the body is empty. Nothing to translate  
3     here.  
4  
5     # recurse  
6     return bisection_rec(x, l, u, e)
```

Recall that in MIPS, a recursive call can be translated as any other function call. **Start the translation with a stack diagram** written as comments at the point of line 3's execution (the translation assumes no body). The clarity of the MIPS code you write will be assessed together with its correctness and faithfulness.

# Appendix

## Information

### MIPS reference sheet for FIT1008 and FIT2085

Table 1: System calls

Call code (\$v0)	Service	Arguments	Returns	Notes
1	Print integer	\$a0 = value to print	-	value is signed
4	Print string	\$a0 = address of string to print	-	string must be terminated with '\0'
5	Input integer	-	\$v0 = entered integer	value is signed
8	Input string	\$a0 = address at which the string will be stored \$a1 = maximum number of characters in the string	-	returns if \$a1-1 characters or Enter typed, the string is terminated with '\0'
9	Allocate memory	\$a0 = number of bytes	\$v0 = address of first byte	-
10	Exit	-	-	ends simulation

Table 2: General-purpose registers

Number	Name	Purpose
R00	\$zero	provides constant zero
R01	\$at	reserved for assembler
R02, R03	\$v0, \$v1	system call code, return value
R04-R07	\$a0--\$a3	system call and function arguments
R08-R15	\$t0--\$t7	temporary storage (caller-saved)
R16-R23	\$s0--\$s7	temporary storage (callee-saved)
R24, R25	\$t8, \$t9	temporary storage (caller-saved)
R28	\$gp	pointer to global area
R29	\$sp	stack pointer
R30	\$fp	frame pointer
R31	\$ra	return address

Table 3: Assembler directives

.data	assemble into data segment
.text	assemble into text (code) segment
.word w1[, w2, ...]	allocate word(s) with initial value(s)
.space n	allocate n bytes of uninitialized, unaligned space
.ascii "string"	allocate ASCII string, do not terminate
.asciiz "string"	allocate ASCII string, terminate with '\0'

Table 4: Function calling convention

On function call:	<b>Caller:</b> saves temporary registers on stack passes arguments on stack calls function using <code>jal fn_label</code>	<b>Callee:</b> saves value of \$ra on stack saves value of \$fp on stack copies \$sp to \$fp allocates local variables on stack
On function return:	<b>Callee:</b> sets \$v0 to return value clears local variables off stack restores saved \$fp off stack restores saved \$ra off stack returns to caller with <code>jr \$ra</code>	<b>Caller:</b> clears arguments off stack restores temporary registers off stack uses return value in \$v0



Table 5: A partial instruction set is provided below. The following conventions apply.

<b>Instruction Format</b> column
<b>Rsrc, Rsrc1, Rsrc2:</b> register source operand(s) - must be the name of a register
<b>Rdest:</b> register destination - must be the name of a register
<b>Addr:</b> address in the form <b>offset(Rsrc)</b> , that is, absolute address = <b>Rsrc + offset</b>
<b>label:</b> label of an instruction
<b>**:</b> pseudoinstruction
<b>Immediate Form</b> column
Associated instruction where <b>Rsrc2</b> is an immediate. Symbol - appears if there is no immediate form.
<b>Unsigned or overflow</b> column
Associated unsigned (or overflow) instruction for the values of <b>Rsrc1</b> and <b>Rsrc2</b> . Symbol - if no such form.

Table 6: Allowed MIPS instruction (and pseudoinstruction) set

Instruction format	Meaning	Operation	Immediate	Unsigned or Overflow
add Rdest, Rsrc1, Rsrc2	Add	$Rdest = Rsrc1 + Rsrc2$	addi	addu (no overflow trap)
sub Rdest, Rsrc1, Rsrc2	Subtract	$Rdest = Rsrc1 - Rsrc2$	-	subu (no overflow trap)
mult Rsrc1, Rsrc2	Multiply	$Hi:Lo = Rsrc1 * Rsrc2$	-	mulu
div Rsrc1, Rsrc2	Divide	$Lo = Rsrc1 / Rsrc2;$ $Hi = Rsrc1 \% Rsrc2$	-	divu
and Rdest, Rsrc1, Rsrc2	Bitwise AND	$Rdest = Rsrc1 \& Rsrc2$	andi	-
or Rdest, Rsrc1, Rsrc2	Bitwise OR	$Rdest = Rsrc1   Rsrc2$	ori	-
xor Rdest, Rsrc1, Rsrc2	Bitwise XOR	$Rdest = Rsrc1 \wedge Rsrc2$	xori	-
nor Rdest, Rsrc1, Rsrc2	Bitwise NOR	$Rdest = \sim(Rsrc1   Rsrc2)$	-	-
sllv Rdest, Rsrc1, Rsrc2	Shift Left Logical	$Rdest = Rsrc1 << Rsrc2$	sll	-
srlv Rdest, Rsrc1, Rsrc2	Shift Right Logical	$Rdest = Rsrc1 >> Rsrc2$ (MSB=0)	srl	-
srav Rdest, Rsrc1, Rsrc2	Shift Right Arithmet.	$Rdest = Rsrc1 >> Rsrc2$ (MSB preserved)	sra	-
mfhi Rdest	Move from Hi	$Rdest = Hi$	-	-
mflo Rdest	Move from Lo	$Rdest = Lo$	-	-
lw Rdest, Addr	Load word	$Rdest = mem32[Addr]$	-	-
sw Rsrc, Addr	Store word	$mem32[Addr] = Rsrc$	-	-
la Rdest, Addr(or label) **	Load Address (for printing strings)	$Rdest = Addr$ (or $Rdest = label$ )	-	-
beq Rsrc1, Rsrc2, label	Branch if equal	if ( $Rsrc1 == Rsrc2$ ) PC = label	-	-
bne Rsrc1, Rsrc2, label	Branch if not equal	if ( $Rsrc1 != Rsrc2$ ) PC = label	-	-
slt Rdest, Rsrc1, Rsrc2	Set if less than	if ( $Rsrc1 < Rsrc2$ ) Rdest = 1 else Rdest = 0	slti	sltu , sltiu
j label	Jump	PC = label	-	-
jal label	Jump and link	$\$ra = PC + 4;$ PC = label	-	-
jr Rsrc	Jump register	PC = Rsrc	-	-
jalr Rsrc	Jump and link register	$\$ra = PC + 4;$ PC = Rsrc	-	-
syscall	system call	depends on the value of \$v0	-	-